

Limesi funkcija

- (1) $\lim_{x \rightarrow -\infty} \frac{2x^2 - 3x + 4}{\sqrt{x^4 + 1}}$
- (2) $\lim_{x \rightarrow +\infty} \frac{(x+2)^3(x^2+x+1)^2}{x^7 - 50x + 5}$
- (3) $\lim_{x \rightarrow +\infty} \frac{\sqrt[3]{x^3 + 2}}{x}$
- (4) $\lim_{x \rightarrow -\infty} \frac{(x-1)^3}{2x^3 - x + 2}$
- (5) $\lim_{x \rightarrow -\infty} \frac{x^2 - 5x + 1}{3x + 7}$
- (6) $\lim_{x \rightarrow +\infty} \frac{\sqrt{x}}{\sqrt{\sqrt{x + \sqrt{x + \sqrt{x}}}}}$
- (7) $\lim_{x \rightarrow 1} \frac{2x^2 - x - 1}{x^2 - 1}$
- (8) $\lim_{x \rightarrow 3} \frac{x^2 - 5x + 6}{x^2 - 8x + 15}$
- (9) $\lim_{x \rightarrow 1} \frac{x^m - 1}{x^n - 1} \quad (m, n \in \mathbb{N})$
- (10) $\lim_{x \rightarrow -1} \frac{1 + \sqrt[5]{x}}{1 + \sqrt[3]{x}}$
- (11) $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{\sqrt[3]{1+x} - 1}$
- (12) $\lim_{x \rightarrow 1} \frac{\sqrt[3]{x} - 1}{\sqrt[4]{x} - 1}$
- (13) $\lim_{x \rightarrow 1} \left(\frac{3}{1-x^3} - \frac{1}{1-x} \right)$
- (14) $\lim_{x \rightarrow 1} \frac{\sqrt[3]{x^2} - 2\sqrt[3]{x} + 1}{(x-1)^2}$
- (15) $\lim_{x \rightarrow 7} \frac{2 - \sqrt{x-3}}{x^2 - 49}$
- (16) $\lim_{x \rightarrow 4} \frac{3 - \sqrt{5+x}}{1 - \sqrt{5-x}}$
- (17) $\lim_{x \rightarrow +\infty} \left(x + \sqrt[3]{1-x^3} \right)$
- (18) $\lim_{x \rightarrow +\infty} \left(\sqrt{x^2 - 5x + 6} - x \right)$
- (19) $\lim_{x \rightarrow +\infty} \left(\sqrt{x^2 + 1} - \sqrt{x^2 - 4x} \right)$
- (20) $\lim_{x \rightarrow -\infty} \frac{\sqrt{x^2 + a^2} + x}{\sqrt{x^2 + b^2} + x} \quad (a, b > 0)$
- (21) $\lim_{x \rightarrow +\infty} \left(\sqrt{x + \sqrt{x + \sqrt{x}}} - \sqrt{x} \right)$
- (22) $\lim_{x \rightarrow \frac{\pi}{4}} \frac{1 - \sin 2x}{1 + \cos 4x}$
- (23) $\lim_{x \rightarrow \pi} \frac{\operatorname{tg} x}{\sin 2x}$
- (24) $\lim_{x \rightarrow \pi} \frac{\sqrt{1 - \operatorname{tg} x} - \sqrt{1 + \operatorname{tg} x}}{\sin 2x}$
- (25) $\lim_{x \rightarrow \frac{\pi}{2}} \left(\frac{\sin x}{\cos^2 x} - \operatorname{tg}^2 x \right)$
- (26) $\lim_{x \rightarrow 0} \frac{\sqrt{x+1} - x - 1}{\sqrt{x+1} - 1}$
- (27) $\lim_{x \rightarrow 4} \frac{\sqrt{1+2x} - 3}{\sqrt{x} - 2}$
- (28) $\lim_{x \rightarrow 0} \frac{x}{\sqrt{1+3x} - 1}$
- (29) $\lim_{x \rightarrow a} \frac{\sqrt[n]{x} - \sqrt[n]{a}}{x - a} \quad (n \in \mathbb{N}, a > 0)$
- (30) $\lim_{x \rightarrow 2} \frac{\sqrt{x} - \sqrt{2}}{x - 2}$

$$(31) \lim_{x \rightarrow 0} \frac{\sin 3x}{x}$$

$$(32) \lim_{x \rightarrow 0} \frac{\sin ax}{\sin bx} \quad (a, b \neq 0)$$

$$(33) \lim_{x \rightarrow \pi} \frac{\sin ax}{\sin bx} \quad (a, b \in \mathbb{N})$$

$$(34) \lim_{x \rightarrow 0} \frac{1 - \cos x}{x^2}$$

$$(35) \lim_{x \rightarrow 0} \frac{1 - \cos^3 x}{x^2}$$

$$(36) \lim_{x \rightarrow 0} \frac{1 - \cos 2x}{x \sin x}$$

$$(37) \lim_{x \rightarrow 0} \frac{\sin^2 \frac{x}{2}}{x^2}$$

$$(38) \lim_{x \rightarrow a} \frac{\sin x - \sin a}{x - a} \quad (a \in \mathbb{R})$$

$$(39) \lim_{x \rightarrow 1} \frac{\sin(x-1)}{1-x^3}$$

$$(40) \lim_{x \rightarrow 0} \frac{\sin(x+1)}{x+1}$$

$$(41) \lim_{x \rightarrow 0} \frac{\sin 4x}{\sqrt{x+1} - 1}$$

$$(42) \lim_{x \rightarrow +\infty} x \sin \frac{\pi}{x}$$

$$(43) \lim_{x \rightarrow +\infty} \frac{\sin x}{x}$$

$$(44) \lim_{x \rightarrow 0} \frac{2 \sin(\sqrt{x+1} - 1)}{x}$$

$$(45) \lim_{x \rightarrow 0} \frac{\sin^2 x}{\sqrt{1+x \sin x} - \cos x}$$

$$(46) \lim_{x \rightarrow \frac{\pi}{3}} \frac{\sin(x - \frac{\pi}{3})}{1 - 2 \cos x}$$

$$(47) \lim_{x \rightarrow 0} \frac{\sqrt[m]{\cos \alpha x} - \sqrt[n]{\cos \beta x}}{x^2} \quad (m, n \in \mathbb{N}, \alpha, \beta \in \mathbb{R})$$

$$(48) \lim_{x \rightarrow 0} \frac{1 - \cos 2x + \operatorname{tg}^2 x}{x \sin x}$$

$$(49) \lim_{x \rightarrow 0} \frac{1 + \sin x - \cos x}{1 + \sin px - \cos px} \quad (p \neq 0)$$

$$(50) \lim_{x \rightarrow 2} \left(\frac{\sin(x-2)}{x^2 - 4} + \frac{1}{(x-2)^2} \right)$$

$$(51) \lim_{x \rightarrow \frac{\pi}{4}} \frac{\sin 4x \cos 2x}{(x - \frac{\pi}{4})^2}$$

$$(52) \lim_{x \rightarrow 0} \frac{\arcsin x}{x}$$

$$(53) \lim_{x \rightarrow 0} \frac{\operatorname{arctg} x}{x}$$

$$(54) \lim_{x \rightarrow \frac{\pi}{4}} \frac{\sqrt{2} \cos x - 1}{1 - \operatorname{tg}^2 x}$$

$$(55) \lim_{x \rightarrow 1} (1-x) \operatorname{tg} \frac{\pi x}{2}$$

$$(56) \lim_{x \rightarrow 0} \frac{\sqrt{1 + \sin x} - \sqrt{1 - \sin x}}{x}$$

$$(57) \lim_{x \rightarrow 0} \frac{\operatorname{ctg}(2x+a) - 2 \operatorname{ctg}(x+a) + \operatorname{ctg} a}{(a \in \mathbb{R} \setminus \{k\pi : k \in \mathbb{Z}\})}$$

$$(58) \lim_{x \rightarrow 0} \frac{\sqrt{\cos x} - \sqrt[3]{\cos x}}{\sin^2 x}$$

$$(59) \lim_{x \rightarrow +\infty} \left(\frac{x+1}{x-1} \right)^x$$

$$(60) \lim_{x \rightarrow 0} (1 + \operatorname{tg} x)^{\operatorname{ctg} x}$$

$$(61) \lim_{x \rightarrow +\infty} \left(\frac{2x+3}{2x+2} \right)^{x+1}$$

$$(62) \lim_{x \rightarrow 0} \frac{a^x - 1}{x} \quad (a > 0)$$

$$(63) \lim_{x \rightarrow 0} \frac{e^{-2x} - 1}{x}$$

$$(64) \lim_{x \rightarrow 0} \frac{e^{ax} - e^{bx}}{x} \quad (a, b \in \mathbb{R})$$

$$(65) \lim_{x \rightarrow 0} \frac{e^x - 1}{\sin x}$$

$$(66) \lim_{x \rightarrow +\infty} x(a^{\frac{1}{x}} - 1) \quad (a > 0)$$

$$(67) \lim_{x \rightarrow 0} \frac{1}{x} \ln \sqrt{\frac{1+x}{1-x}}$$

$$(68) \lim_{x \rightarrow \frac{\pi}{4}} \frac{\ln \operatorname{tg} x}{\cos 2x}$$

$$(69) \lim_{x \rightarrow 0} (\cos x)^{\frac{1}{\sin^2 x}}$$

$$(70) \lim_{x \rightarrow 0} (\cos x)^{\frac{1}{x}}$$

$$(71) \lim_{x \rightarrow 0} (\cos x)^{\frac{1}{x^2}}$$

$$(72) \lim_{x \rightarrow 0} (1 + \sin x)^{\frac{1}{x}}$$

$$(73) \lim_{x \rightarrow 0} \frac{\ln \cos x}{x^2}$$

$$(74) \lim_{x \rightarrow 0} \frac{\log(1 + 10x)}{x}$$

$$(75) \lim_{x \rightarrow 0} \frac{\ln(x+2) - \ln 2}{x}$$

$$(76) \lim_{x \rightarrow 0} \frac{8^x - 7^x}{6^x - 5^x}$$

$$(77) \lim_{x \rightarrow +\infty} \frac{2^x + 3}{2^x - 3}$$

$$(78) \lim_{x \rightarrow -\infty} \frac{2^x + 3}{2^x - 3}$$

$$(79) \lim_{x \rightarrow 1} \frac{x^x - 1}{x \ln x}$$

$$(80) \lim_{x \rightarrow 0} \frac{(1+x)^a - 1}{x} \quad (a \in \mathbb{R})$$

$$(81) \lim_{x \rightarrow 0} \frac{1 - \cos^a x}{x^2} \quad (a \in \mathbb{R})$$

$$(82) \lim_{x \rightarrow a} \frac{a^{ax} - a^{xa}}{a^x - x^a} \quad (a > 0)$$

$$(83) \lim_{x \rightarrow a} \frac{a^x - x^a}{x - a} \quad (a > 0)$$

$$(84) \lim_{x \rightarrow -\infty} \frac{\ln(1 + 5^x)}{\ln(1 + 3^x)}$$

$$(85) \lim_{x \rightarrow +\infty} \arcsin \frac{1-x}{1+x}$$

$$(86) \lim_{x \rightarrow 0} \frac{(e^{x^2} - 1)^2 + x^2}{\cos x - 1 - \frac{1}{2}x^2}$$

$$(87) \lim_{x \rightarrow e} \left(\frac{a^{\ln x} + b^{\ln x}}{a + b} \right)^{\frac{1}{\ln x - 1}} \quad (a, b > 0)$$

$$(88) \lim_{x \rightarrow 0} (\cos 4x)^{\frac{3}{2e^{3x} - 2}}$$

$$(89) \lim_{x \rightarrow 0} (\cos 3x)^{\frac{2}{\operatorname{th}^2 3x}}$$

$$(90) \lim_{x \rightarrow 0} \frac{\sqrt{\cos 2x} \cdot e^{3x^2} - 1}{x \operatorname{th} 4x}$$

$$(91) \lim_{x \rightarrow 0} \frac{(1+x^2)e^{\frac{3}{2}x^2} - 1}{x \sin 2x}$$

$$(92) \lim_{x \rightarrow 0} \frac{\sin(1 - \cos(2\sqrt{2}x))}{\pi x^2}$$

$$(93) \lim_{x \rightarrow 0} \frac{\cos(\sin x) - \cos x}{x^2}$$

$$(94) \lim_{x \rightarrow 0} \frac{1 - \cos(1 - \cos x)}{(1 - \cos x)^2}$$

$$(95) \lim_{x \rightarrow +\infty} \frac{\sqrt{x \operatorname{sh} x} - e^x}{2 \operatorname{ch} x}$$

$$(96) \lim_{x \rightarrow -\infty} \frac{\sqrt{x \operatorname{sh} x} - e^x}{2 \operatorname{ch} x}$$

$$(97) \lim_{x \rightarrow +\infty} \left(\ln x - \frac{1}{2} \ln(x^2 + 3) \right)$$

$$(98) \lim_{x \rightarrow 0} \left(\frac{1}{\sin^2 x} - \frac{1}{4 \sin^2 \frac{x}{2}} \right)$$

$$(99) \lim_{x \rightarrow +\infty} \frac{(x \operatorname{sh} x)^2}{8^x}$$

$$(100) \lim_{x \rightarrow +\infty} \frac{x^{1000} \operatorname{ch}^4 x}{100^x}$$

$$(101) \lim_{x \rightarrow 0} \frac{x^2}{\sqrt[5]{1+5x} - 1 - x}$$

$$(102) \lim_{x \rightarrow +\infty} \left(\sqrt[3]{x^3 + 3x^2} - \sqrt{x^2 - 2x} \right)$$

$$(103) \lim_{x \rightarrow +\infty} \frac{(x - \sqrt{x^2 - 1})^n + (x + \sqrt{x^2 - 1})^n}{x^n} \\ (n \in \mathbb{N})$$

$$(104) \lim_{x \rightarrow \frac{\pi}{6}} \frac{2 \sin^2 x + \sin x - 1}{2 \sin^2 x - 3 \sin x + 1}$$

$$(105) \lim_{x \rightarrow \frac{\pi}{3}} \frac{\operatorname{tg}^3 x - 3 \operatorname{tg} x}{\cos(x + \frac{\pi}{6})}$$

$$(106) \lim_{x \rightarrow 0} \frac{\operatorname{tg}(a+x) \operatorname{tg}(a-x) - \operatorname{tg}^2 a}{x^2} \\ (a \in \mathbb{R} \setminus \{ \frac{\pi}{2} + k\pi : k \in \mathbb{Z} \})$$

$$(107) \lim_{x \rightarrow 0} \left(\frac{1 + \operatorname{tg} x}{1 + \sin x} \right)^{\frac{1}{\sin x}}$$

$$(108) \lim_{x \rightarrow 0} \left(\frac{1 + \operatorname{tg} x}{1 + \sin x} \right)^{\frac{1}{\sin^3 x}}$$

$$(109) \lim_{x \rightarrow +\infty} \left(\sin \frac{1}{x} + \cos \frac{1}{x} \right)^x$$

$$(110) \lim_{x \rightarrow +\infty} \frac{\ln(x^2 - x + 1)}{\ln(x^{10} + x + 1)}$$

$$(111) \lim_{x \rightarrow 0} \frac{\ln(a+x) + \ln(a-x) - 2 \ln a}{x^2} \\ (a > 0)$$

$$(112) \lim_{x \rightarrow 0} \frac{e^{x^2} - (\cos x)^{\sqrt{2}}}{x^2}$$

$$(113) \lim_{x \rightarrow 1} \frac{\sin(\pi x^\alpha)}{\sin(\pi x^\beta)} \quad (\alpha, \beta \neq 0)$$

$$(114) \lim_{x \rightarrow 1} \frac{\sin^2(\pi 2^x)}{\ln \cos(\pi 2^x)}$$

$$(115) \lim_{x \rightarrow \pi} (2 + \cos x)^{(x-\pi)^{-2}}$$

$$(116) \lim_{x \rightarrow \frac{\pi}{2}} (\sin x)^{\cos^{-2} x}$$

$$(117) \lim_{x \rightarrow \pi} \left(\frac{2\pi x - x^2}{\pi^2} \right)^{\operatorname{ctg}^2 x}$$

$$(118) \lim_{x \rightarrow 0} \frac{\sin(e^{3 \operatorname{arctg} x} - e^{2 \sin x})}{\ln(1 + \arcsin x)}$$

$$(119) \lim_{x \rightarrow 0} (e^{\operatorname{arctg} x} - e^{\arcsin x}) \cdot \frac{\sin x}{1 - \cos^3 x}$$

$$(120) \lim_{x \rightarrow 0} \frac{\sin(e^{1-\cos^3 x} - e^{1-\cos^4 x})}{x \operatorname{arctg} x}$$

$$(121) \lim_{x \rightarrow 0} \frac{e^{\sin^2 x} - e^{1-\cos^3 x}}{x \ln(1 + \operatorname{arctg} x)}$$

$$(122) \lim_{x \rightarrow 0} \frac{\sin(\sin(\sin(\sin x)))}{\operatorname{tg}(\operatorname{tg}(\operatorname{tg}(\operatorname{tg} x)))}$$

$$(123) \lim_{x \rightarrow 0} \frac{\operatorname{tg}(\operatorname{tg} x) - \sin(\sin x)}{\operatorname{tg} x - \sin x}$$